

DEPARTMENT OF PHYSICS, UIO

FYS3610-SPACE PHYSICS

MID-TERM EXAMINATION

Date: October 10, 2005

Time of day: 13:30-15:30 (2 hours!)

Permitted aid(s): Calculating machine.

The set consists of 4 pages, with 3 Problems.

NOTE: At page 4 you find a Table with some numbers and equations that might be useful.

Problem 1

THE ATMOSPHERE

- a) The Earth atmosphere is subdivided in regions according to the temperature altitude profile. Draw a temperature versus altitude profile with realistic scales. Annotate the different regions by name. Point out the heat sources along this profile.
- b) The barometric equation for an isothermal atmosphere is given as:

$$p = p_0 \cdot e^{-\frac{mg}{kT} z}$$

Show how to derive this equation. Define the scale height. What is the typical scale height in the meteorological region?

- c) Draw a figure that qualitatively demonstrates the Chapman layer variations with altitude z and zenith angle χ .

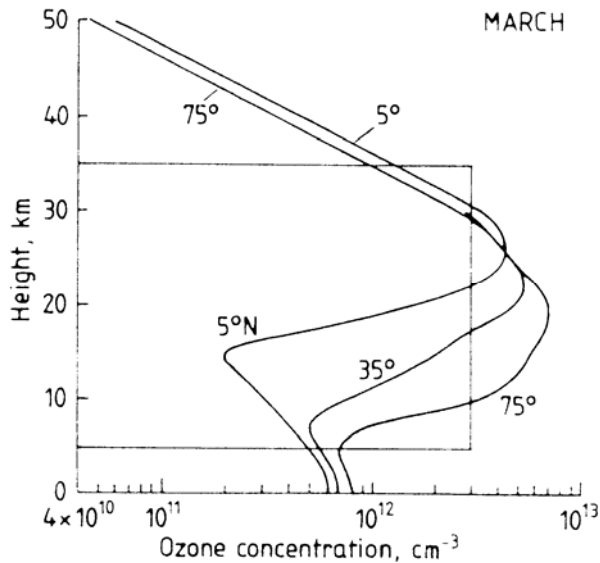


Figure 1

- d) Describe Figure 1 above. Explain the latitude variation of the peak magnitude and peak altitude.

Problem 2

THE EARTH MAGNETIC FIELD AND PARTICLE MOTION

The Lorentz force on a charged particle is given as :

$$\vec{F}_L = q\vec{E} + q\vec{v} \times \vec{B}$$

- a) In the absence of an electric field, show that a charged particle's motion can be resolved into two components: one along the magnetic field and one perpendicular to the magnetic field.
- b) Show that the gyro radius is given by $r_c = \frac{mv_{\perp}}{qB}$ and that the gyrofrequency is

$$\text{given by } \omega_c = \frac{qB}{m}$$

- c) Calculate the gyrofrequencies (in hertz) of proton and an electron in a 100-nT field, a 1000 nT field and a 10.000 nT field. At roughly what distances from Earth centre can these gyrofrequencies be found in the equatorial plane (see Table for information about the Earth's magnetic field)?
- d) What is the gyroradius of a proton moving with transverse to a 100 nT magnetic field at $2 \times 10^5 \text{ ms}^{-1}$? How does this distance compare with the distance in the

equatorial plane over which the Earth's dipole field changes from 100 nT to 200 nT (a factor 2)?

Problem 3

THE SUN

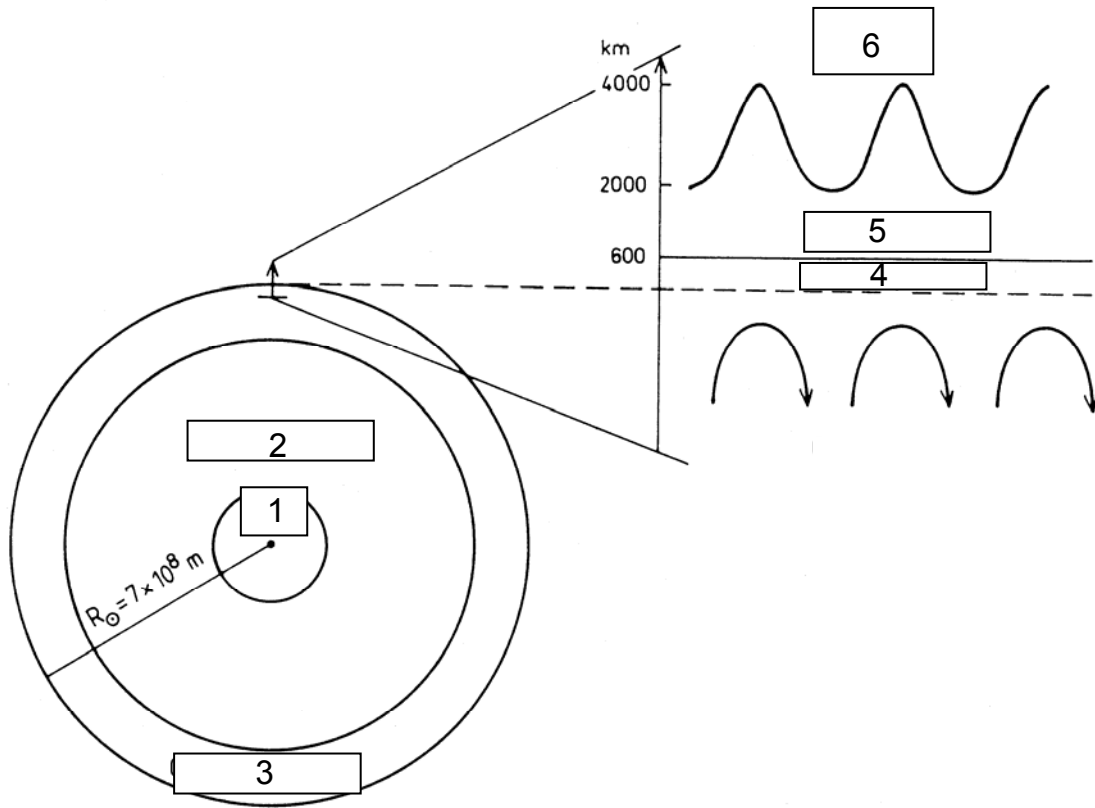


Figure 2

- Name different regions 1- 6 in Figure 2.
- Give a brief characteristics of sunspots (where do they occur, magnetic field, temperature, 11-year cycle).
- The solar radius is 6.960×10^5 km; the Sun weights 1.989×10^{30} kg. What is the escape velocity?
- The Sun emits 3.9×10^{26} Js^{-1} . If all the energy emitted comes from fusion in the core, how much mass is burned off per second of the Sun? How long will it take to burn off 1% of the mass?

e) The total radiated power from the Sun is:

$$Q_S = 4\pi R_S^2 E_S = 3.9 \times 10^{26} \text{ W}$$

Show that the radiated energy per unit area at 1 AU (1.496×10^8 km) is 1380 Wm^{-2} .

List of equations and numbers:

$$E = mc^2$$

$$B_{Eq} = B_0 \left(\frac{R_E}{r} \right)^3$$

$$E = -\frac{GMm}{r}$$

$$\rho = nm$$

$$a_c = \frac{v_{\perp}^2}{r}$$

$$B_0 = 30000nT$$

$$R_E = 6400km$$

$$R_S = 6.960 \times 10^5 \text{ km}$$

$$1 \text{ AU} = 1.496 \times 10^8 \text{ km}$$

$$|q| = e = 1.6 \times 10^{-19} \text{ C}$$

$$G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$$

$$k = 1.38 \times 10^{-23} \text{ J K}^{-1}$$

$$m_p = 1.67 \times 10^{-27} \text{ kg}$$

$$m_e = 9.1 \times 10^{-31} \text{ kg}$$

$$c = 3 \times 10^8 \text{ ms}^{-1}$$